



### **Inference of Robust Reachability Constraints**

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### **Automatic Bug Detection**

**Programs have bugs** 

Bugs can be exploited  $\rightarrow$  Vulnerabilities

We need automated methods to detect bugs

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### **Example: Symbolic Execution**

- Explore the program paths
- Finds program input that exhibits the bug
- Sound: no false positives

### **Automatic Bug Detection**



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**Bugs can be exploited** → **Vulnerabilities** 

We need automated methods to detect bugs

### • Vulnerabilities • Fin

**Example: Symbolic Execution** 

- Finds program input that exhibits the bug
- Sound: no false positives





```
Example
void g() {
    uint a = read();
    uint b; /* uninitialized */
    if (a + b == 0)
        /* bug */
    else
    ...
}
Symbolic Execution?
```

• Very easy: a = 0, b = 0



#### 

### The Issue

- Depends on uncontrolled initial value (b)
- The formal result is not reliably reproducible

### Symbolic Execution?

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#### Example

}
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. . .

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### **Practical Causes of Unreliable Assignments**

- Interaction with the environment
- Stack canaries
- Uninitialized memory/register dependency
- Choice of undefined behaviors

We need to characterize the replicability of bugs



#### ldea

- Partition of the input space
  - What is controlled
  - What is uncontrolled





#### Idea

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### Focus: Reliable Bugs

 Controlled input that triggers the bug independently of the value of the uncontrolled inputs





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#### **Extension of Reachability and Symbolic Execution**

```
void g() {
    uint a = read();
    uint b; /* uninitialized */
    if (a + b == 0)
         /* bug */
    else
         . . .
}
    controlled
                      uncontrolled
        Ξ
                 A
           а
                    b
                        error
     Not Robustly Reachable
```

### 

### Example 3

- Memcopy with slow and fast path
- Fast path is buggy but slow path is not

typedef struct { unsigned char bytes[32]; } uint256\_t;

```
void memcpy(void* dst, const void* src, size_t n) {
    if (((dst | src | n) & 0b11111))
        /* slow path */
        for (size_t i = 0; i < n; i += 1)
            dst[i] = src[i];
    else /* fast path */
        for (size_t i = 0; i <= (n >> 5); i += 1)
            (uint256_t*)dst[i] = (uint256_t*)src[i];
}
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#### memory alignment constraint

#### Example 3

- Memcopy with slow and fast path
- Fast path is buggy but slow path is not
- Reachability: Vulnerable
- Robust Reachability: Not reliably triggerable
  - Taking the fast path depends on uncontrolled initial values



The bug is serious but not robustly reachable – The concept is too strong

### **Robust Reachability Constraints**

#### Definition

 Predicate on program input sufficient to have Robust Reachability typedef struct { unsigned char bytes[32]; } uint256\_t;

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#### <u>Lea</u> Inference of Robust Reachability Constraints

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\exists * src, \forall src, dst, src \% 32 = 0 \land dst \% 32 = 0 \Rightarrow overflow
```

(src and dst aligned on 32bits)

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### **Robust Reachability Constraints**

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 Predicate on program input sufficient to have Robust Reachability

#### **Advantages**

- Part of the Robust Reachability framework
- Allows precise characterization

typedef struct { unsigned char bytes[32]; } uint256\_t;

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    if (((dst | src | n) & 0b1111))
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How to Automatically Generate Such Constraints?

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### **Contributions**



- New program-level abduction algorithm for Robust Reachability Constraints Inference
  - Extends and generalizes Robustness, made more practical
  - Adapts and generalizes theory-agnostic logical abduction algorithm
  - Efficient optimization strategies for solving practical problems
- Implementation of a restriction to Reachability and Robust Reachability
  - First evaluation of software verification and security benchmarks
  - Detailed vulnerability characterization analysis in a fault injection security scenario

**Target:** Computation of  $\phi$  such that  $\exists$  *C* controlled value,  $\forall$  *U* uncontrolled value,  $\phi(C, U) \Rightarrow reach(C, U)$ 

#### **Abductive Reasoning**

[Josephson and Josephson, 1994]

- Find missing precondition of unexplained goal
- Compute  $\phi_M$  in  $\phi_H \land \phi_M \vDash \phi_G$

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### **Theory-Specific Abduction**

[Bienvenu 2007, Tourret et. al. 2017]

• Handle a single theory

### **Specification Synthesis**

[Albarghouthi et. al. 2016, Calcagno et. al. 2009, Zhou et. al. 2021]

• White-box program analysis

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#### **Theory-Agnostic First-order Abduction**

[Echenim et al. 2018, Reynolds et al. 2020]

- Efficient procedures
- Genericity

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Our Proposal: Adapt Theory-Agnostic Abduction Algorithm to Compute Program-level Robust Reachability Constraints

- Program-level
- Generic



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## G Inference Language (Set of Candidates) Abduct

**Our Solution (Framework)** 

 $\rightarrow P$  Program

- $\psi$  Target Trace Predicate
- $\mathcal{A}_C$  Memory Partition



#### **Oracles on Trace Properties**

Robust property queries

•

- $O^{\exists \forall}$  $O^{\exists \exists}$
- Non-robust property queries
- Can accomodate various tools (SE, BMC, Incorrectness, ...)

Robust Reachability Constraints

### **Our Solution (Baseline Algorithm)**



Theorem:

- **Termination** when the oracles terminate
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- Under correction and completeness of the oracles
  - **Minimality** w.r.t. the inference language
  - Weakest constraint generation when expressible

### **Making it Work**



#### The Issue

• Exhaustive exploration of the inference language is inefficient

#### Key Strategies for Efficient Exploration

- Necessary constraints
- Counter-examples for Robust Reachability
- Ordering candidates

### **Making it Work: Necessary Constraints**

#### The Idea

• Find and store Necessary Constraints





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### Usage

- Build a candidate solution faster
- Additional information on the bug
- Emulate unsat core usage in the context of oracles





### **Making it Work: Counter-Examples**

#### The Idea

• Reuse information from failed candidate checks

#### The Issue

 Non Robustness (∀∃ quantification) does not give us counter-examples





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### Proposal

- Use a second trace property that ensures the bug does not arise
- Prune using these counter-examples



### **Experimental Evaluation**



#### Implementation **BINSEC**

- (Robust) Reachability on binaries
- Tool: **BINSEC** [Djoudi and Bardin 2015]
- Tool: **BINSEC/RSE** [Girol at. al. 2020]

#### Prototype

- PyAbd, Python implementation of the procedure
- Candidates: Conjunctions of equalities and disequalities on memory bytes

### **Research Questions**

- 1) Can we compute non-trivial constraints?
- 2) Can we compute weakest constraints?
- 3) What are the algorithmic performances?
- 4) Are the optimization effective?

### Benchmarks

- Software verification (SVComp extract + compile)
- Security evaluation (FISSC, fault injection)

### **Results: Generating Constraints**

	SV-COM	$P(E_{\mathcal{G}})$	SV-CON	sv-comp $(I_{\mathcal{G}})$		sc $(E_{\mathcal{G}})$	FISSC $(I_{\mathcal{G}})$		
# programs	147	64	147	64	719	719	719	719	
# of robust cases	111	3	111	3	129	118	129	118	
# of sufficient rrc	122	5	127	24	359	598	351	589	
# of weakest rrc	111	3	120	4	262	526	261	518	

#### **Inference languages**

- (dis-)Equality between memory bytes  $(E_{\mathcal{G}})$
- + Inequality between memory bytes  $(I_{\mathcal{G}}) \rightarrow$
- More expressivity but more candidates

previous

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									proviouo
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- (dis-)Equality between memory bytes  $(E_{\mathcal{G}})$ •
- $(I_{\mathcal{G}})$ + Inequality between memory bytes  $\rightarrow$ ٠

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#### We can find more reliable bugs than Robust Symbolic Execution

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our characterization

### **Benchmark: FISSC**

#### **Fault Injection Attacks**

- Physical perturbation of the system executing the program
- Changes the program behavior
- Introduces new bugs
- How does each method characterize these bugs?

#### VerifyPINs

- 10 protected implementations
- 4800 faulted binary programs



	PyAbd <sup>P</sup>	Binsec/RSE	Binsec	Qemu	Qemu+l
unknown	170	273	170	243	284
not vulnerable (0 input)	4042	4419	3921	4398	4220
vulnerable ( $\geq 1$ input)	598	118	719	169	306
≥ 0.0001%	598	118	_	_	306
$\geq 0.01\%$	582	118	_	_	281
$\geq 0.1\%$	514	118	_	_	210
$\geq 1.0\%$	472	118	_	_	199
$\geq 5.0\%$	471	118	_	_	196
$\geq 10.0\%$	401	118	_	_	148
$\geq 50.0\%$	401	118	_	_	135
100.0%	399	118	_	_	135

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Many reported vulnerabilities

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### **Results: Example of Constraints**

• true

Authentication is always possible

Card[0] == User[0] && User[0] == 3

Authentication when first digit is 3

- User[0] == User[1] && User[0] == User[2] && User[0] == User[3] && User[0] != 0
   Authentication when all digits are equal and non zero
- Card[2] != User[2] && Card[3] == User[3] && User[1] == 5
   Authentication when we know the last digit, the 3rd is not correct and the 2<sup>nd</sup> is 5.
- R0 == User[3] && User[3] == User[2] && User[3] == User[1] && User[3] == User[0]
   Authentication with four time the initial value of R0
- R2 = 0xaa && R1 != 0x55 && R1 != 0

Authentication if R2=0xaa initially and R1 distinct from both 0x55 and 0x00 initially

**BINSEC** 

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## Conclusion

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- We propose a precondition inference technique to ٠ improve the capabilities of Robust Reachability
- We adapt theory-agnostic abduction algorithm to  $\exists \forall$ ٠ formulas and apply it at program-level through oracles
- We demonstrates its capabilities on simple yet realistic ٠ vulnerability characterization scenarii





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Preconditions **explain** the vulnerability Can be reused for understanding, counting, comparing







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### **Questions?**

Also, we have open positions





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## BINSEC

