

# Precise and efficient memory analysis for low level languages

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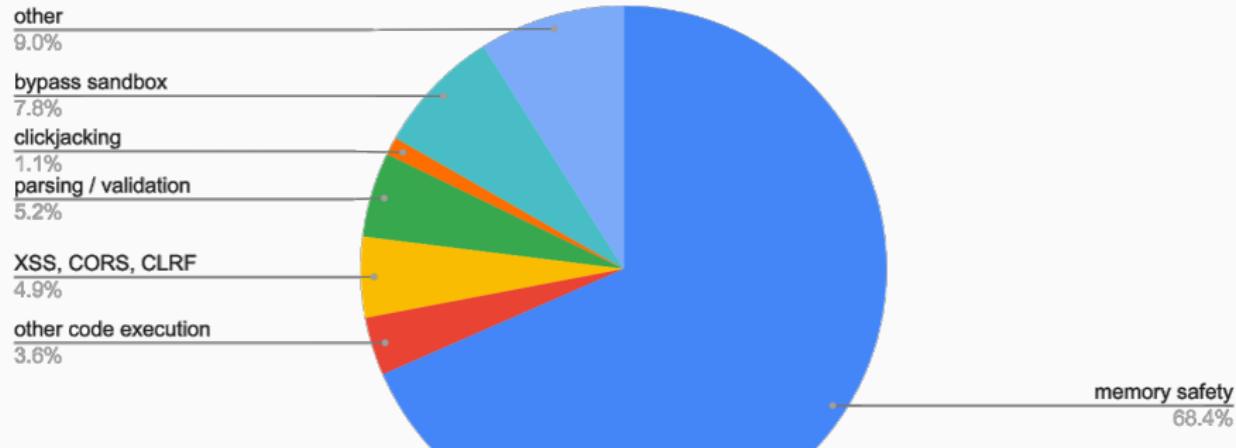
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Working Group: "Formal Methods for Security" (GT MFS)

# Memory safety



CVE vulnerabilities in Flash Player: <https://ultrasaurus.com/2019/12/memory-safety-necessary-not-sufficient>

~~null pointer dereferencing~~

~~array out of bounds~~

~~use after free~~

# Low-level languages



01100  
10110  
11110



## Common idioms

- Hand-coded variant types
- Separated array and size
- Bitwise operations on addresses

## Objective

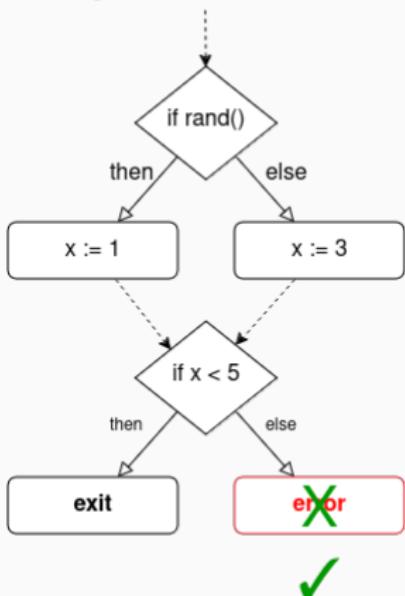
Develop an automated static analysis method:

- Efficient and precise
- For the verification of low-level programs without modification
- Ensuring spatial memory safety

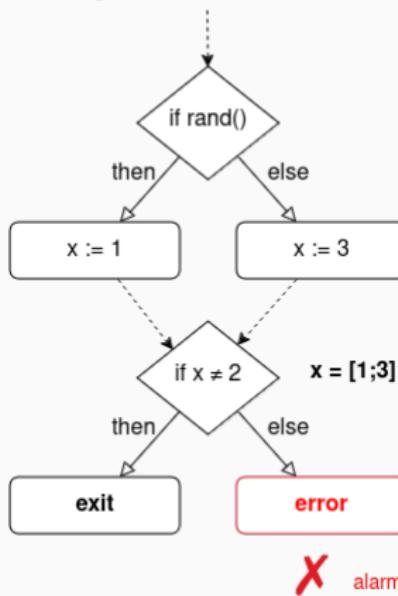
# Abstract interpretation

Abstract interpretation is an automatic verification method based on abstract domains that over-approximate sets of concrete states.

Program 1



Program 2



definitively valid

possibly false

## Our approach

Static analysis using abstract interpretation with a domain based on a new **dependent** type system, which provides:

- Expressive invariants over memory
- Cheap analysis operations
- Easy configuration
- Modular (per-function) analysis

Checking type safety (by abstract interpretation) guarantees spatial memory safety

# Examples

## Example 1 : Bit-stealing

```
1 struct Lisp_Cons {  
2     int car ;  
3     int cdr ;  
4 };  
5 ...  
6 if ((p & 7) == 3)  
7     (Lisp_Cons*)(p-3)->cdr = p;
```

32	0	3	0
	Lisp_Cons*	0	
p =	Lisp_Cons*	3	

Valid program that uses  
bit-stealing

## Example 2 : Buffer

```
1 struct {  
2     int size ;  
3     char* buffer;  
4 };  
5 ...  
6 x->size = 3;  
7 x->buffer = malloc(3);  
8 for (i=0;i<5;i++)  
9     x->buffer[i] = 0; ← alarm 1  
10 x->size++; ← alarm 2
```

The program contains:

1. A store outside the array
2. A type error

# Record & array types

Types represent a memory layout.

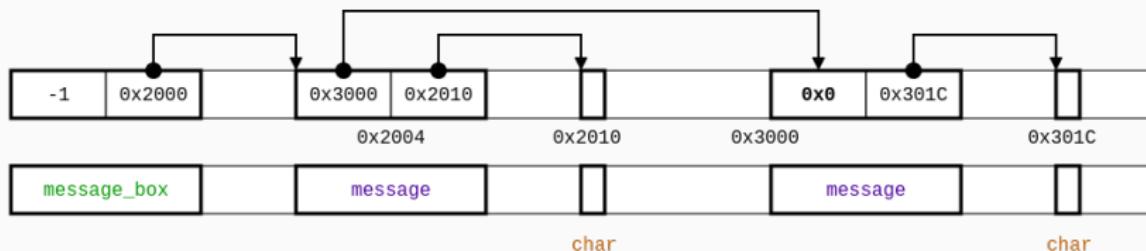
**Record types**  $\tau_1 \times \tau_2$  and **array types**  $\tau[e]$  concatenate types.

```
def int := byte[4]
def char := byte

def message :=
    message* ×
    char*

def message_box :=
    byte[4] ×
    message*
```

```
1 struct message {
2     struct message *next;
3     char *buffer;
4 };
5
6 struct message_box {
7     int length;
8     struct message *first;
9 };
```



# Refinement types

Types also represent values.

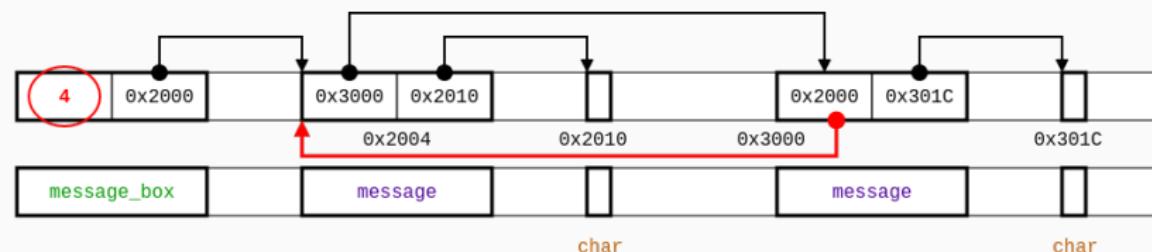
Values in a **refinement type**  $\tau$  with  $p$  fulfill predicate  $p$ .

```
def int := byte[4]
def char := byte

def message :=
    message* ×
    char*

def message_box :=
    byte[4] with self >= 0 ×
    message*
```

```
1 struct message {
2     struct message *next;
3     char *buffer;
4 };
5
6 struct message_box {
7     int length;
8     struct message *first;
9 };
```



# Existential types

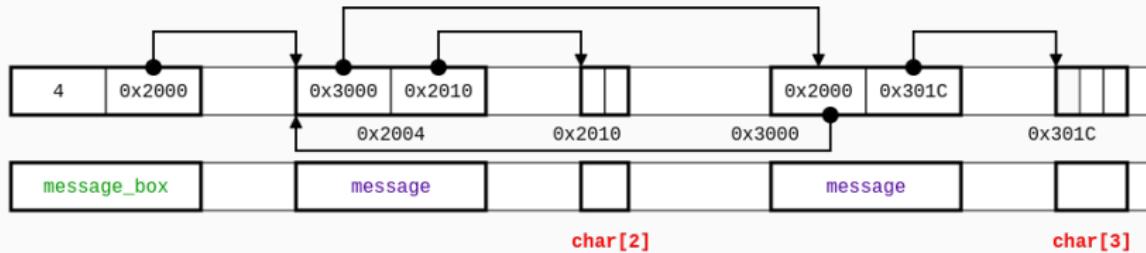
**Existential types**  $\exists \alpha : \tau_1.\tau_2$  introduce a **symbolic variable**  $\alpha$  of type  $\tau_2$ .

```
def int := byte[4]
def char := byte

def message :=
  len:byte[4] with self >= 0.
  message* ×
  char[len]*

def message_box :=
  byte[4] with self >= 0 ×
  message*
```

```
1 struct message {
2   struct message *next;
3   char *buffer;
4 };
5
6 struct message_box {
7   int length;
8   struct message *first;
9 };
```



# Parameterized types

Parameterized types  $\tau_a(e_1, \dots, e_n)$  use symbolic variables as parameters.

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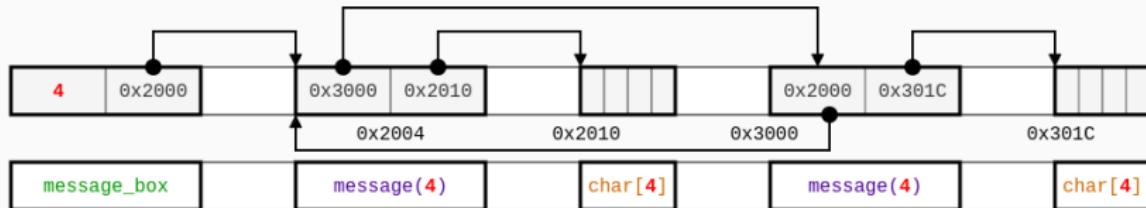
```
def int := byte[4]
def char := byte

def message(len:int) :=
    message(len)* ×
    char[len]*

def message_box :=
    ∃ mlen:byte[4] with self >= 0.
    byte[4] self = mlen ×
    message(mlen)*
```

---

```
1 struct message {
2     struct message *next;
3     char *buffer;
4 };
5
6 struct message_box {
7     int length;
8     struct message *first;
9 };
```



# Union types

**Union types**  $\tau_1 \cup \tau_2$  specify that a value belong to one type or the other (or both).

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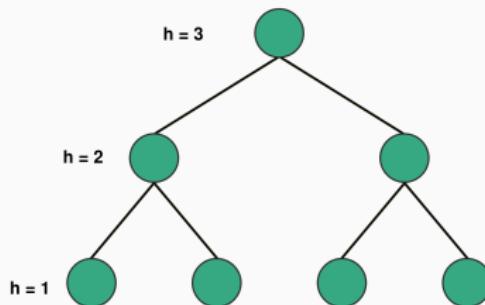
```
def node(h) :=
    byte[4] ×
    ((node(h-1)* × node(h-1)*) with h > 0
    ∪ (nullptr × nullptr) with h ≤ 0)

def nodeptr :=
    ∃ h:byte[4] with self > 0. node(h)*
```

---

```
1 struct node {
2     int value;
3     struct node *left;
4     struct node *right;
5 };
```

This specifies a perfect binary tree



# Nominal type system

Pointer types  $\eta^*$  point to a **name**  $\eta$

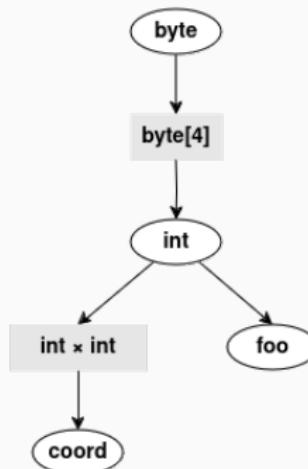
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```
def int := byte[4]
def coord := int × int
def foo := int
```

---

## Derivation rules

- $(|coord^*|) \subseteq (|int^*|)$
- $(|foo^*|) \subseteq (|int^*|)$
- $(|coord^*|) \cap (|foo^*|) = \emptyset$



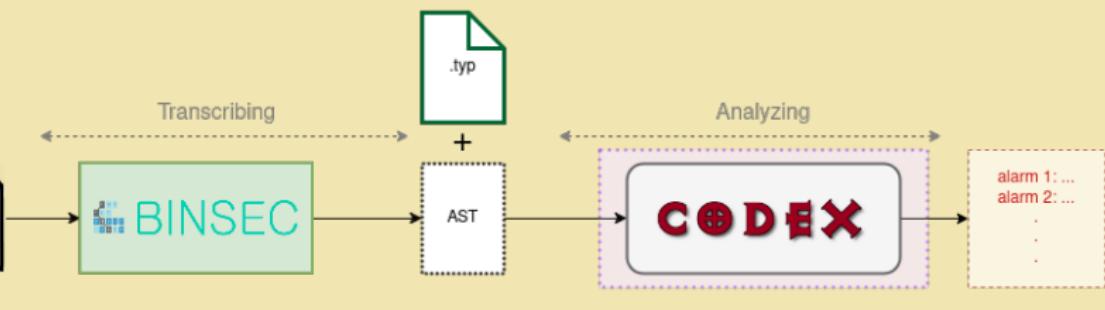
# Complete type system

Our complete system is the following:

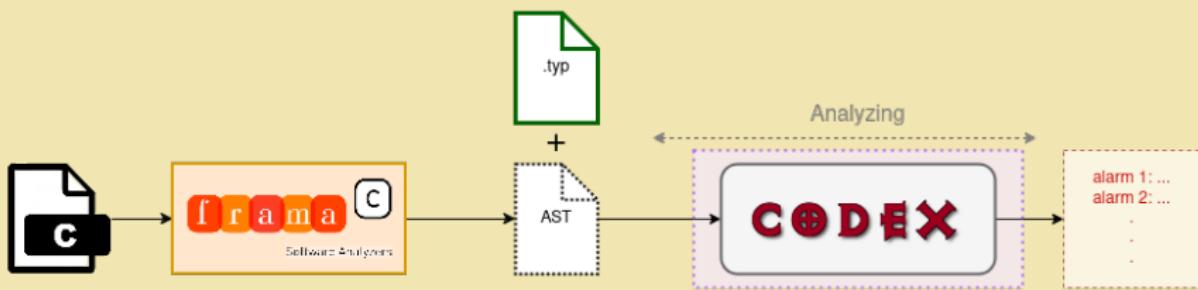
$\tau$	$::=$	$\text{byte}$	(basic type of a single byte)
		$\eta$	(type name)
		$\eta^*$	(non null pointer type)
		$\tau_1 \times \tau_2$	(product type)
		$\tau \text{ with } e$	(refinement type)
		$\tau[e]$	(array type)
		$\tau_a(e_1, \dots, e_n)$	(application of a constructor)
		$\exists \alpha : \tau_1. \tau_2$	(existential type)
		$\tau_1 \cup \tau_2$	(union type)
		$\tau_1 \wedge \tau_2$	(intersection type)
$\tau_a$		$::=$	$\eta(\alpha : \tau_1). \tau_2$ (type constructor)

# Codex, an automatic interprocedural analysis engine

## Binary code analysis



## C code analysis



# Evaluation

## Code patterns

(BS) bit-stealing

(FAM) flexible array member

(DU) discriminated variant types

(IP) interior pointers

(NLI) non-local invariants

(P?) possibly null pointer

Case studies	#LoC	#Entry	Code patterns						#Spec		#Alarms			Time (s)
			BS	DU	NLI	FAM	IP	P?	gen	man	gen	final	true	
OS	Contiki	329	12	-	-	-	-	✓	19	14	16	2	0	1.33
	QDS <sup>bin</sup>	401	3	-	✓	✓	-	-	83	83	18	0	0	1.28
	RBTree	1 111	2	-	-	-	-	✓	29	17	5	2	0	0.46
Emacs	list <sup>bin</sup>	464	8	✓	✓	-	-	-	✓		-	0	0	3.03
	string <sup>bin</sup>	109	5	✓	✓	✓	-	-	✓	73	-	5	0	3.20
	buffer <sup>bin</sup>	42	3	✓	✓	-	✓	-	✓		-	0	0	3.12
Shapes	Graph	155	7	-	-	-	-	-	26	14	0	0	0	0.79
	Javl	920	9	-	-	-	-	-	37	34	10	1	1	0.70
	Kennedy	197	6	-	-	-	-	✓	44	24	6	0	0	0.74
	RBtree	978	7	-	-	-	-	-	32	18	56	16	0	0.42
	(6-)Other	5 742	19	-	-	-	-	-	113	50	27	5	0	3.79

# Comparison with CheckedC

CheckedC is the state-of-the-art verification tool by Microsoft.

Case studies (Olden)	#LoC	#Entry	Code patterns						CC+3C		#Spec		#Alarms			Time (s)
			BS	DU	NLI	FAM	IP	P?	man	gen	man	gen	gen	final	true	
bh <sup>c</sup>	2 107	30	-	✓	-	-	-	✓	181	18	27	144	9	3	1	26.04
bisort <sup>c</sup>	356	11	-	✓	-	-	✓	✓	92	34	29	29	9	0	0	2.18
em3d <sup>c</sup>	693	17	-	-	✓	-	-	✓	158	88	50	53	42	15	0	6.48
health <sup>c</sup>	486	12	-	-	-	-	-	✓	99	57	37	57	14	4	0	5.96
mst <sup>c</sup>	431	6	-	✓	-	-	-	✓	161	28	16	44	33	10	3	1.89
perimeter <sup>c</sup>	486	7	-	✓	-	-	-	✓	44	10	26	41	13	1	0	1.64
power <sup>c</sup>	618	17	-	-	-	-	-	✓	83	20	26	75	29	4	0	6.04
treadd <sup>c</sup>	249	2	-	-	-	-	-	✓	46	16	0	19	0	0	0	0.42
tsp <sup>c</sup>	617	11	-	-	✓	-	-	✓	78	10	0	32	0	0	0	3.86
voronoi <sup>c</sup>	1 151	40	✓	-	-	-	-	✓	✗	✗	37	101	57	49	0	21.35

## Codex vs. CheckedC

### Pros

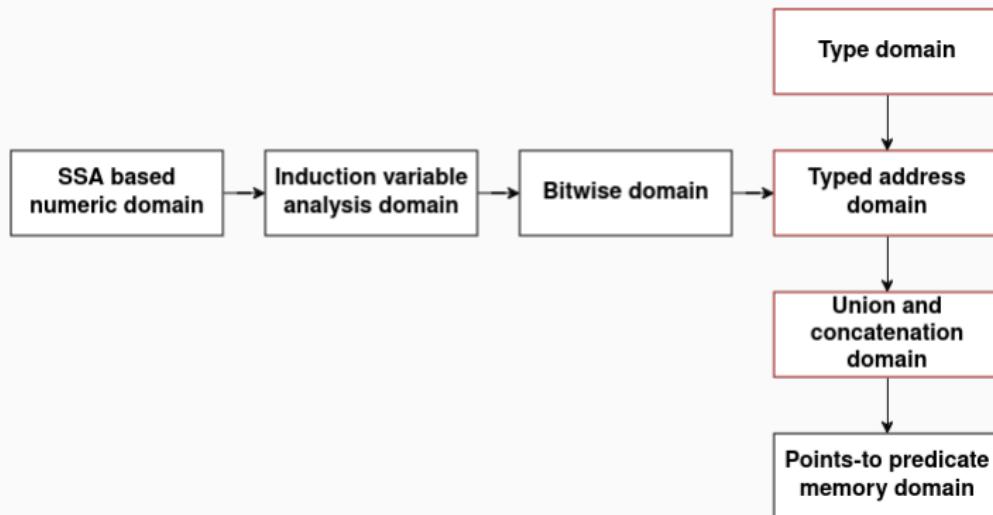
- + could still crash in CheckedC
- + overhead in CheckedC
- + detects null pointer deferences
- + works on unmodified programs
- + supports union types

### Cons

- specification need an understanding of programs
- still some imprecision to solve (with the tool)

# Implementation overview

This work is combined with additionnal work on abstract interpretation:



As well as support for interprocedural and higher order analysis.

# Conclusion

## Summary

- Type checking by abstract interpretation
  - Automated inference from assembly to typed assembly
  - Automated proof of spatial memory safety for C and machine code
- Novel type system with many interesting properties
- Evaluation on challenging low-level code patterns

## Future work

- Improve automation (infer specification)
- Improve precision (domains for strings and arrays)
- Verify temporal memory safety (use-after-free errors)
- Resubmit paper 

**Questions?**